Spiral curves are generally used to provide a gradual change in curvature from a straight section of road to a curved section. They assist the driver by providing a natural path to follow. Spiral curves also improve the appearance of circular curves by reducing the break in alignment perceived by drivers. Figure 1 shows the placement of spiral curves in relation to circular curves. Figure 2 shows the components of a spiral curve.

Figure 1: Placement of spiral curve.

Figure 2: Components of a spiral curve.
Definitions

SCS PI = Point of intersection of main tangents.
TS = Point of change from tangent to spiral curve.
SC = Point of change from spiral curve to circular curve.
CS = Point of change from circular curve to spiral curve.
ST = Point of change from spiral curve to tangent.
LC = Long chord.
LT = Long tangent.
ST = Short tangent.
PC = Point of curvature for the adjoining circular curve.
PT = Point of tangency for the adjoining circular curve.
Ts = Tangent distance from TS to SCS PI or ST to SCS PI.
Es = External distance from the SCS PI to the center of the circular curve.
Rc = Radius of the adjoining circular curve.
Dc = Degree of curve of the adjoining circular curve, based on a 100 foot arc (English units only).
D = Degree of curve of the spiral at any point, based on a 100 foot arc (English units only).
I = Spiral arc from the TS to any point on the spiral (I = Ls at the SC).
Ls = Total length of spiral curve from TS to SC (typically the superelevation runoff length, see Section 2A-2 and Section 2A-3).

L = Length of the adjoining circular curve.
θs (or Theta) = Central (or spiral) angle of arc Ls.
Δ = Total central angle of the circular curve from TS to ST.
Δc = Central angle of circular curve of length L extending from SC to CS.
p = Offset from the initial tangent.
k = Abscissa of the distance between the shifted PC and TS.
Yc = Tangent offset at the SC.
Xc = Tangent distance at the SC.
x and y = coordinates of any point on the spiral from the TS.
Chapter 2—Alignments

Section 2C-1—Spiral Curves

Formulas

\[
D_c = \frac{18000}{R_c} \quad \text{R}_c \text{ given in feet, } D_c \text{ in decimal degrees}
\]

\[
D_c = 200 \times \frac{\theta_s}{L_s} \quad \theta_s \text{ and } D_c \text{ in decimal degrees, } L_s \text{ in feet}
\]

\[
L_s = 200 \times \frac{\theta_s}{D_c} \quad \theta_s \text{ and } D_c \text{ in decimal degrees, } L_s \text{ in feet}
\]

\[
\theta_s = \frac{L_s \times D_c}{200} \quad \theta_s \text{ in decimal degrees, } L_s \text{ in feet}
\]

\[
\Delta = \frac{180 \times L}{\pi \times R_c} \quad L \text{ and } R_c \text{ in feet}
\]

\[
\theta_s = \frac{L_s}{2 \times R_c} \quad \theta_s \text{ in radians, } L_s \text{ and } R_c \text{ in feet}
\]

\[
X_c = \left( \frac{L_s}{100} \right) \times (100 - 0.0030462(\theta_s)^2) \quad \theta_s \text{ in decimal degrees, } L_s \text{ in feet}
\]

\[
Y_c = \left( \frac{L_s}{100} \right) \times (0.58178\theta_s - 0.000012659(\theta_s)^3) \quad \theta_s \text{ in decimal degrees, } L_s \text{ in feet}
\]

\[
p = Y_c - R_c \times (1.0 - \cos \theta_s) \quad Y_c, R_c, \text{ and } p \text{ in feet and } \theta_s \text{ in decimal degrees}
\]

\[
A = \frac{20000 \times \theta_s}{L_s^2} \quad A \text{ and } L_s \text{ in feet, } \theta_s \text{ in decimal degrees}
\]

\[
k = \frac{1}{2}L_s - 0.000127A^2 \times \left( \frac{L_s}{100} \right)^5 \quad A \text{ and } L_s \text{ in feet}
\]

\[
T_s = (R_c + p) \times \tan \frac{\Delta}{2} + k \quad T_s, R_c, p, \text{ and } k \text{ in feet, } \Delta \text{ in decimal degrees}
\]

\[
E_s = (R_c + p) \times \text{exsec} \frac{\Delta}{2} + p \quad \text{Es, } R_c, \text{ p, and } k \text{ in feet, } \Delta \text{ in decimal degrees, and exsec}\alpha \text{ is defined as } (\tan\alpha) \left( \tan \frac{1}{2} \alpha \right)
\]

\[
LT = X_c - (Y_c \times \cot \theta_s) \quad LT, X_c, \text{ and } Y_c \text{ in feet, } \theta_s \text{ in decimal degrees}
\]

\[
ST = \frac{Y_c}{\sin \theta_s} \quad ST \text{ and } Y_c \text{ in feet, } \theta_s \text{ in decimal degrees}
\]

\[
LC = L_s - 0.00034A^2 \times \left( \frac{L_s}{100} \right)^5 \quad LC, A \text{ and } L_s \text{ in feet}
\]

\[
\Delta_c = \Delta - 2 \times \theta_s \quad \Delta_c, \Delta \text{ and } \theta_s \text{ measured in decimal degrees}
\]
Spiral Curves on Bridges

Spiral curves should be avoided on bridges. The designer should select a curve radius which doesn’t require a spiral curve. The designer should contact the Methods Section for additional assistance on removing spiral curves from bridges.

Plan Curve Data

Provide the following Spiral Curve Data on the plan and profile sheets for each spiral curve: $\Delta$, $E_s$, $T_s$, $L_s$, $\theta_s$, $P$, $K$, $X_c$, $Y_c$, $LT$, $ST$, $LC$, and SCS PI stationing.

Curve data, superelvation data, and coordinates of each control point should be shown within the G sheets on tabulations 101-16 and 101-17.

Spiral curve data should be displayed in following order on plan sheets:

SCS PI Sta.
$\Delta =$
Theta =
$L_s =$
$T_s =$
$E_s =$
$P =$
$K =$
$X_c =$
$Y_c =$
$LT =$
$ST =$
$LC =$
5/28/2010 Revised
Add language about removing spiral curves from bridges. Removed metric formulas. Added language on displaying curve data in plans. Deleted requirement for spirals with superelevation of 3% or greater (new requirements are covered in 2A-2).

1/29/2010 Revised
Update to current standards